Modes in silver-iodide-lined hollow metallic waveguides mapped by terahertz near-field time-domain microscopy

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Thin dielectric layers inside hollow metallic waveguides are used to improve the waveguide transmission characteristics as the dominant waveguide mode changes into the hybrid HE11 mode. We investigate the effect of 1 μm thick silver iodide (AgI) coatings on the fundamental modes in cylindrical waveguides at terahertz (THz) frequencies, in the regime of the dielectric layer being thinner than the optimal thickness h_opt (2 THz) = 20 μm. In the region of 1–3.2 THz, the lowest-order modes are similar in profile to the TE01 and TM11 modes, as determined by the time-resolved near-field measurements and verified numerically. Higher-order modes are detected experimentally as mode mixtures due to the multimode propagation. Numerical electromagnetic modeling is applied to resolve the mode structure ambiguity, allowing us to correlate experimentally detected patterns with a superposition of the TM11 and the higher-order mode, TE12. Mode profiles determined here indicate that in the regime of ultrathin dielectric (h ∝ 0.1λTHz), the dielectric layer does not transform the dominant mode into the low-loss HE11 mode. Experimental mode patterns similar to the HE11 and the TE01 modes nevertheless can be formed due to mode beating. The results indicate that the Ag/AgI waveguides can be used for guiding THz waves in the TE01 mode or the TE12 mode with high discrimination against other modes. © 2012 Optical Society of America

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1. INTRODUCTION

Significant contributions to the development of terahertz (THz) dielectric-lined hollow cylindrical waveguides (also described as hollow circular waveguides) have been made by both the microwave and optical communities [1]. Experimental and theoretical development in this area started in the millimeter-wave regime [2–4]. In light of the high losses suffered by the TE01 of the traditional rectangular waveguides and the transverse electromagnetic mode of coaxial waveguides, microwave engineers shifted their interest to cylindrical waveguides and their TE0ν modes (where ν is an integer and denotes radial variation) because of their low attenuation at high frequencies [5]. However, the TE01 mode is degenerate with the highly lossy TM11 mode, and researchers then examined strategies to break this degeneracy by, for instance, corrugations [6,7] or dielectric coatings [2,4,8,9]. Corrugations and dielectric inclusions were also designed to transform the TE11 eigenmode of the cylindrical waveguide to the optical-fiber-like hybrid HE11 mode. This hybrid mode is well confined in the hollow core of the waveguide, with the propagation loss and attenuation due to bends smaller than for the TE01 [2,3,10,11]. Moreover, unlike the TE01 mode, the linearly polarized HE11 mode facilitates the conversion to a free-space linearly polarized Gaussian beam. Corrugated waveguides have been the mainstream in high-energy science where strong interaction with an axial electron flux is pursued [12,13] and an active line in antenna research [6,14]. Dielectric-lined cylindrical waveguides were meanwhile developed for communication systems [2–4]; however, they were abandoned later in favor of optical fibers. These waveguides were recuperated subsequently for high-power delivery as well as for surgical applications with midinfrared lasers [15,16]. In this regime, extensive analytical work revealed the complex development of the hybrid HE11 mode and the evolution of the other relevant modes [10,15,17,18]. The dielectric-lined waveguide technology for infrared waves has paved the way for reducing propagation losses in THz waveguides [1,19].

Microwave, infrared, and optical regions have mature technologies as a result of extensive development. However, in the THz band, i.e., from 0.3 to 3 THz, components, system architectures, and experimental techniques are still emerging. In the quest to develop the THz band, THz waveguides has become an active research area [20]. The oversized corrugated and dielectric-lined cylindrical waveguides reviewed above are attractive candidates for low-loss transmission of THz waves. However, simply scaling corrugated microwave technology for THz frequencies would require extremely challenging dimensions. The fabrication difficulty for the corrugated waveguides was recently addressed by a smart arrangement of stacked rings at 0.26 THz [21]. The dielectric-lined hollow metallic waveguides, on the other hand, can be flexible and can be fabricated at low cost [16]. In addition, in the
mid- and far-infrared regions, they display lower losses than solid dielectric waveguides. Among the possible dielectric films available to be deposited as inner coating, silver iodide (AgI) has been extensively studied \[22,23\]. The reason for this choice relies on several factors: AgI is (i) nontoxic, (ii) heat resistant, (iii) highly transparent throughout the whole infrared spectrum, and (iv) compatible with Ag films. This metal is the favored material for the metallization of the hollow glass and polymer tubing. Ag has the lowest damping constant among noble metals; i.e., it is a relatively good conductor even at midinfrared. Ag toxicity is almost negligible compared to nickel, copper, or aluminum. These properties and the developed fabrication technology make the AgI-based hollow waveguides attractive for THz applications. However, increasing the thickness of the deposited dielectric is the major obstacle to extending the AgI-lined hollow metallic waveguide technology to THz waves, for which the optimal thickness is $10–40 \mu m$ \[24\].

In this manuscript, we address the impact of the AgI coating on the mode structure and transmission losses for THz waveguides in the regime of the coating being much thinner than the wavelength. Recently the Ag waveguides with a relatively thin $1 \mu m$ AgI coating were tested for transmitting THz waves \[25\]. The experimental results indicated the formation of the low-loss hybrid HE\(_{11}\) mode \[25\]. The thickness of the AgI coating was, however, much smaller than the estimated optimum thickness for THz frequencies \[24\]. In this regime, modal and dispersion properties of Ag/AgI THz waveguides have not been addressed thoroughly yet. Here, we combine numerical calculations with experimental THz near-field time-resolved mode analysis and continuous-wave (CW) mode analysis to characterize the ultrathin AgI-lined cylindrical metallic waveguides. Note that we classify dielectric films with thickness $h \ll 0.1 \lambda_{opt}$ as the ultrathin dielectrics. For comparison purposes, we also show the properties of a smooth cylindrical metallic waveguide with similar dimensions. The results obtained here also provide insight into far-field CW mode characterization at THz frequencies \[25,26,27\].

2. EXPERIMENTAL SETUPS AND MODELING

The experimental time-domain setup is based on a THz time-domain spectroscopy (TDS) system as described in \[28–31\]. The waveguide sample part of the setup is shown in Fig. 1. The incident horizontally polarized ($E_x$) THz pulse generated via optical rectification is launched from the left-hand side of Fig. 1 and collimated by an Si lens (3 mm diameter). The beam is incident on a waveguide sample placed at a distance shorter than 1 mm from the lens. The THz pulse couples to the waveguide modes, which propagate along the waveguide and generate certain time-dependent field patterns at the output. In order to match the circularly centrosymmetric THz beam efficiently to the fundamental waveguide mode, TE\(_{11}\), and to minimize the excitation of higher-order modes, the $xy$-position of the input waveguide facet is adjusted while monitoring the output field pattern. This procedure can also be used for optimum excitation of higher-order modes, e.g., the TE\(_{03}\) mode \[1,21\]. The waveguide output is mounted on an automated translation stage and placed in close proximity to a near-field THz probe with an integrated subwavelength (10 \mu m) aperture \[30\]. Spatial distribution of the guided THz wave is determined by scanning the waveguide output end with respect to the probe. The change in the coupling conditions at the waveguide input during the scan is negligible because the maximum tilt of the waveguide input in this experiment is \(\lesssim 1\) deg. This system allows us to measure the output THz pulse in time (using the optical time-delay stage of the THz TDS system) at any $xy$-position of the output facet of the waveguide as described in \[1,30,31\]. It enables us to generate space-time maps, which elucidate the arrival time for waveguide modes, and two-dimensional (2D) distributions of the electric-field component $E_y(x,y)$ of the output THz pulse at any chosen time delay.

For CW experimental characterization, a microring distributed-feedback quantum cascade laser operating at 3.2 THz is used as a source. The vertically emitting microring laser has a diameter $d_l = 990 \mu m$ (fabrication details are described in \[27\]). The device is biased, using six bonding wires along the ring. The latter procedure allows the single-mode operation and constant polarization along the whole quantum cascade laser ring. The laser is mounted on the cold finger of a liquid-helium cryostat and driven at currents of 2.04 A with 200 ns wide pulses and with an effective 0.5% duty cycle. A Picarin lens (3 cm focal length) is used to focus the azimuthally polarized THz beam into a 1 mm large pinhole kept in contact with the waveguide input. A calibrated pyroelectric detector (sensitive area about 3 mm\(^2\)) is mounted on a $xy$-translation stage to record the far-field distribution of radiation at a distance of \(\approx 2\) cm from the waveguide output.

The waveguide in this study is a 1 mm inner bore diameter dielectric-lined hollow cylindrical metallic waveguide \[16,25,32\]. The AgI coating is estimated to be $1.0 \pm 0.2 \mu m$ thick via the analysis of interference absorption peaks using Fourier-transform infrared spectroscopy; the waveguide sample length is $80 \pm 1\) mm and $140 \pm 1\) mm for the time-domain and CW experiments, respectively. To evaluate the effect of the AgI coating, a series of time-domain experiments is also performed on a similar waveguide without the AgI coating.

Before one can understand the experimental results presented here, it is helpful to review the eigenmodes supported by the hollow cylindrical metallic waveguides with and without an ultrathin dielectric coating. Although the latter
waveguide has an exact analytical solution [5], the former does not and only approximations exist under certain conditions [3,15,17,18,33]. Therefore, in order to model the experiment accurately, we calculate numerically the eigenmodes and the corresponding eigenvalues (dispersion diagram) of both waveguides with the 2D eigenmode solver of CST Microwave Studio™.

A nonuniform tetrahedral mesh is used rather than a hexahedral grid to map accurately the curvature and the dielectric region of the cylindrical waveguide without heavy demand on computational resources. The maximum and minimum edge lengths of the tetrahedral mesh for the uncoated waveguide are 45.5 and 6.4 μm, respectively. For the AgI-lined waveguide, a mesh refinement has been employed on the AgI coating leading to maximum and minimum edge lengths of 38.5 and 0.4 μm, respectively. The metal, silver, is modeled with a conductivity \( \sigma_{Ag} = 6.3012 \times 10^7 \text{ S/m} \), whereas the AgI is considered to have a relative permittivity \( \varepsilon_r' = 2.3 \) and loss tangent \( \tan \delta = \varepsilon_r''/\varepsilon_r' = 0.001 \). To the best of our knowledge, AgI has not been characterized at the frequencies of interest of this work, and thus, the chosen loss tangent is a conjecture founded on the typical values for dielectric films at THz frequencies. Needless to say, the full-wave simulation of the whole setup or even the 80 mm long waveguide alone would lead to inaccessible computation effort.

Figure 2 shows the attenuation constant for the \( \text{TE}_{11}, \text{TM}_{11}, \) and \( \text{TE}_{12} \) modes of the smooth (metal only) waveguide and for similar modes in the AgI-lined waveguide. Notice that the first 10 modes from the lowest upward are \( \text{TE}_{11}, \text{TM}_{01}, \text{TE}_{21}, \text{TM}_{11}, \text{TE}_{03}, \text{TE}_{31}, \text{TM}_{21}, \text{TE}_{41}, \text{TE}_{12}, \) and \( \text{TM}_{02} \) [34]. However, we restrict the numerical analysis to the aforementioned three modes since they are the most likely excited modes under the on-center symmetrical illumination in our experimental system [20]. The 1 μm thick coating has a significant impact on the attenuation coefficient of the modes [Fig. 2(a)], especially for the \( \text{TE}_{11} \) mode and the \( \text{TM}_{11} \) mode, which have a significant fraction of the mode energy distributed near the waveguide walls [Fig. 2(b)]. For instance, at 2 THz [the central frequency of the THz pulses in our experiment; see Fig. 3(a)], the attenuation coefficient for the \( \text{TE}_{11} \) mode increases from 7.08 to 9.75 dB/m when the AgI coating is introduced [35]. This increase can be understood qualitatively by inspecting the electric-field distribution \( E_x(x, y) \), which shows that the strength of the field on the waveguide walls is larger in the case of the walls coated with a thin dielectric [top row of Fig. 2(b)]. The attenuation coefficient of the \( \text{TM}_{11} \) rises from 16.63 to 17.86 dB/m. This mode, however, remains almost unaltered when the AgI coating is introduced. The attenuation of the \( \text{TM}_{11} \) can arguably be expressed as the sum of the

Fig. 2. (Color online) Numerical results for the uncoated (left) and AgI-coated (right) hollow cylindrical metallic waveguide (1 mm diameter). (a) Attenuation coefficient of the modes observed in the experiments: \( \text{TE}_{11} \) (black curve), \( \text{TM}_{11} \) (red curve), and \( \text{TE}_{12} \) (blue curve) from the lowest to the highest cutoff frequency, respectively. (b) Electric-field lines \( E_x(x, y) \) and \( E_y(x, y) \) color map of the aforementioned modes at 2 THz. From top to bottom: \( \text{TE}_{11}, \text{TM}_{11}, \) and \( \text{TE}_{12} \). The circle in the field-vector diagram represents the dielectric coating. The white and the black dashed curves show the contour of equal intensity for the uncoated and AgI-coated waveguide, respectively. To underline the change in ellipticity of the \( \text{TE}_{11} \) mode, the contour line for the uncoated is also included on the color map for the AgI-coated waveguide.
attenuation constant of the mode in a metallic waveguide and additional loss due to absorption in the AgI-coating [middle row of Fig. 2(b)] [24]. The TE_{12}, on the contrary, does not suffer any significant increment of the attenuation constant. This mode does not see the influence of the dielectric as a result of its confinement to the center of the waveguide. These heuristic arguments are analytically founded [15,17,18,24].

Dispersion characteristics for the TE_{11}, TM_{11}, and TE_{12} modes in both waveguides are displayed in Fig. 3(b) in the form of modal group time delay, $\Delta t_m$. This delay is computed as $\Delta t_m = l/v_g$, where $l$ is the length of the waveguide and $v_g$ is the group velocity. The numerical results show that the 1 $\mu$m thick coating has, however, a small effect on the dispersion characteristic of these modes at THz frequencies. Indeed, this is also confirmed by inspection of the electric-field lines $E(x, y)$ and the electric-field component $E_x(x, y)$; see Fig. 2(b). From these electric-field distributions, one can detect that the fundamental mode in the AgI-coated waveguide is not as oval as in the uncoated waveguide [top row of Fig. 2(b)], whereas the other two modes remain without any appreciable alteration [middle and bottom rows of Fig. 2(b)]. For thinner dielectrics, the modal and dispersion properties of the AgI-lined cylindrical waveguide approach those of the smooth metallic cylindrical waveguide [15,17,18]. For thicker layers, the normal modes are modified to a larger extent. In particular, for the dielectric layer of few tens of micrometers, the HE_{11} mode forms within our frequency range [24,30,31].

After this initial numerical analysis we expect the TE_{11}, TM_{11}, and TE_{12} modes to appear within the first 14 ps (after the arrival of the THz pulse in free space) for the 80 mm
waveguide. Therefore, the experimental data displayed next will be shown in the time-delay span from 0 to 14 ps.

3. EXPERIMENTAL RESULTS AND DISCUSSION

A. Space-Time Mapping of Waveguide Modes

As we have shown previously [13,30,31], the time-resolved near-field mode imaging system allows us to unveil experimentally the waveguide modal characteristics. In this section we discuss the experimental characteristics of the dielectric-lined waveguides in the regime of ultrathin dielectric, for which the existing analytical approximation breaks down. The time-dependent x-component of the electric field, \( E_x \), along the horizontal \((x-)\) and vertical \((y-)\) axes is displayed in Figs. 3(c) and 3(e) and in Figs. 3(d) and 3(f), respectively, for the two test waveguides. Note that \( \Delta t \) corresponds to the time delay with respect to free-space propagation. \( \Delta t \) was calibrated in the experiment for the metal-only waveguide. For the metallic waveguide, the experimental delay is matched to the delay experienced by the TE\(_{11} \) mode at the frequency of 2 THz after propagation through the 80 mm long waveguide.

The regions of intense waves in the maps displayed in Fig. 3 reveal the propagation of different modes. The prominent pulse at the delay \( \Delta t = 0.5-1.5 \) ps unquestionably corresponds to the fundamental mode TE\(_{11} \), which has the fastest group velocity among all eigenmodes. Notice that this mode tends to vanish after 3 ps because the spectral components associated with later delay times fall below the 1.5–2.5 THz bandwidth [see Fig. 3(b), yellow shading]. We can equally well link the early arriving mode to the TE\(_{11} \) based on the spatial profile. According to the eigenmode analysis [Fig. 2(b)], the \( E_x \) of the TE\(_{11} \) expands uniformly along the whole horizontal axis, whereas it drops well before reaching the top and bottom parts of the waveguide. This unique profile is clearly recovered by our experimental space-time maps of Figs. 3(c) and 3(d). It is not surprising that the TE\(_{11} \) carries most of the energy since a circularly centrosymmetric beam has the highest correlation with the TE\(_{11} \) [12–14,20].

A TE\(_{11} \)-like mode is also present in the Ag/AgI waveguide. The visible delay in the dielectric-lined waveguide compared to the metal-only waveguide reflects slightly different group velocities for the dominant modes in the two waveguides. In accordance with the theory of dielectric-lined or corrugated waveguides [2–4,8,15–18], the coating, even as thin as in our case, slows down the mode propagation. This is evident by comparing the 2D color plots of Figs. 3(c)–3(f), and it is emphasized in the top panel of Fig. 3(b), where the numerically computed modal group time delays for the uncoated and coated waveguide are displayed together. Experimentally, the TE\(_{11} \)-like mode in the coated waveguide sample arrives around 0.13 ps after the TE\(_{11} \) mode in the metal-only sample, whereas the modeling predicted 0.08 ps. The slight disagreement can be arguably assigned to the deviation of the estimated dielectric thickness and the modeled relative dielectric permittivity from the real values, pulse reshaping, and experimental uncertainties, such as roughness of the dielectric, which is known to affect the propagation of the modes [19].

It is worth mentioning that we have measured consistently around 50% lower amplitude of the TE\(_{11} \) for the AgI-coated waveguide compared to the uncoated one (after the optimization of the input conditions for each case). This is in qualitative accordance with the numerically computed attenuation coefficient analysis of Fig. 2(a); the TE\(_{11} \) experiences higher attenuation for the AgI-coated waveguide. Although the higher attenuation can be detected in our experiment, we note that quantitative evaluation of the loss in this waveguide requires longer waveguide samples (~100 cm) in order to achieve a sufficient accuracy of \( \pm 0.5 \) dB/m.

Other modes arise after the TE\(_{11} \) mode. Around \( \Delta t = 4 \) ps, one can identify the distinctive spatio-temporal profile of the TM\(_{11} \) mode along horizontal and vertical axes. In the \( xt \) map, the electric field in the center \( E_x(x \sim 0, y = 0) \) and near the edges \( E_x(x \sim \pm 400 \mu\text{m}, y = 0) \) is out of phase, whereas in the \( yt \) map the electric-field component \( E_x(x = 0, y) \) reaches a maximum around \( y = 0 \) and decays toward the edges of the waveguides. This distribution along the principal axes is in agreement with Fig. 2(b). The color pattern beyond \( \Delta t = 6 \) ps could be traced to the TE\(_{12} \)-mode pattern displayed in Fig. 2(b). The reader is referred to Figs. 3(e) and 3(f) for this mode because it has a higher relative amplitude in the AgI-coated waveguide. In the \( yt \)-map [Fig. 3(d)], the wavefront displays phase changes near \( y = \pm 200 \mu\text{m} \) in the region of \( \Delta t = 6–14 \) ps. Meanwhile, the strength of the field reaches a maximum at the waveguide center and diminishes continuously at the walls in the \( xt \)-map [Fig. 3(c)]. Such a profile is consistent with the TE\(_{12} \) mode [Fig. 2(d)]. The TE\(_{12} \) mode is also more confined along \( x \) than the TM\(_{11} \) mode along the \( y \)-axis and the TE\(_{11} \) mode along any of the principal axes.

According to the numerically computed modal time delay for frequencies 1.5–2.5 THz, we expect a mixture of the TM\(_{11} \) and TE\(_{12} \) modes (of different frequencies) within 6–10 ps. Indeed, this can be envisaged in the space-time maps by comparing comprehensively the time spans from 6 to 10 ps and from 10 to 14 ps. The former time span has a less uniform wave pattern due to the beatings of the two modes. In the next section we will confirm the beating of the TM\(_{11} \) and TE\(_{12} \) mode within the time span 6–10 ps by examining the wave spatial profiles (\( xy \)-maps).

As a final remark of this section, we note that the relative magnitude of the TE\(_{12} \) mode (and the admixture TM\(_{11} + \text{TE}_{12} \)) with respect to the TE\(_{11} \) mode is larger for the AgI-coated waveguide than for the uncoated waveguide. This is a direct consequence of the smaller effect that the dielectric coating has on the TE\(_{12} \) mode losses compared to the effect on the TE\(_{11} \) mode losses [Fig. 2(a)]. The ultrathin AgI-coated waveguide could be then exploited advantageously for TE\(_{12} \) mode propagation if it could be excited selectively. To this end, spatial light modulators or off-center illumination, as we have already shown for selective TE\(_{01} \)-mode excitation (see Fig. 1 of [31]), can be used.

B. Near-Field and Far-Field Waveguide Mode Imaging

The identification of modes with the help of \( xt \)- and \( yt \)-maps is effective when the modal structure is known. However, this analysis does not give clear conclusions in complex situations of multimode propagation and for waveguides with an unknown mode structure. In such cases, images of spatial distribution of the electric-field component \( E_x(x, y) \) are required. Even with the spatially and temporally resolved waveforms, we will see in this section that numerical analysis is required
to achieve a full interpretation of the experimental results for the higher-order modes.

Figure 4 displays the 2D distribution of the electric-field component \( E_x(x,y) \) for different time delays. At \( \sim 1.5 \) ps the field patterns for both waveguides account for the dominant TE\(_{11} \) mode [similar to the computed modes in Fig. 2(b)]. The profiles at \( \sim 4.8 \) ps resemble the TM\(_{11} \) mode with the side lobes out of phase with respect to the center spot. These two time delays correspond to the single-mode scenarios, and hence, the straightforward correlation between numerical and experimental results. However, at \( \sim 7.5 \) ps, the field patterns for both waveguides show a concentric disk + ring configuration, which is different from the calculated normal modes (Fig. 2). The field distribution in the AgI-coated waveguide is reminiscent of the TE\(_{12} \), but the field distribution for the uncoated waveguide is certainly different from any of the modes supported by the waveguide.

Now the usefulness of the numerical work becomes evident. First of all, the time-resolved near-field mode map cannot be linked to any numerically computed mode. Second, the modal time delays for the given spectrum suggest the presence of several modes for the time delays larger than 4 ps. Therefore, it is reasonable to explain the observed patterns as a superposition of at least two modes. The modal dispersion results [Fig. 3(b)] restrict the attention to a limited number of modes. At 7.5 ps our attention should be put to the TE\(_{12} \), TM\(_{11} \), TE\(_{01} \), TM\(_{31} \), TE\(_{12} \), and TM\(_{00} \) modes. However, we can limit the selection of modes further because the experimental setup favors coupling into the TM\(_{11} \) and TE\(_{12} \) modes [20]. Therefore, we can expect the experimental patterns in Fig. 4 as the admixture: \( a \cdot E_x^{TM_{11}} + b \cdot E_x^{TE_{12}} \). The combinations of \( a = -0.07 \) and \( b = 0.9975 \) for the uncoated waveguide and \( a = 0.05 \) and \( b = 0.9987 \) for the AgI-coated waveguide match perfectly the experimental time-resolved near-field maps in Fig. 4(c). Note that the relative amplitude coefficients \( a \) and \( b \) are found by a fitting procedure and are scaled to satisfy \( a^2 + b^2 = 1 \) and the minus sign accounts for the 180° phase shift. We emphasize that \( a \) and \( b \) can be interpreted as the relative mode amplitudes only for the purpose of mode analysis at a selected time delay \( \Delta t \). Values of these coefficients vary with the time delay because each mode is described by a unique temporal envelope. Consequently, the different weights of the admixture for the uncoated and coated waveguides should not be attributed solely to losses due to the AgI coating [3]. The coefficients also depend on the relative group and phase delays between the modes.

We can also infer that the TM\(_{11} \) and TE\(_{12} \) modes should be present in the admixture by simple inspection of the color maps in Fig. 4(c). The images show an antinode in the waveguide center. Only the TM\(_{11} \) and TE\(_{12} \) modes (among the modes that are present at \( \Delta t = 7.5 \) ps) exhibit the antinode. Therefore the admixture should have at least one of these modes. The other clue comes from the in-phase ring. In order to convert side lobes of the TM\(_{11} \) mode into a ring, a mode pattern with the in-phase top and bottom lobes is required. The only one in the list is the TE\(_{12} \) mode. Likewise, in order to close an outer ring using the TE\(_{12} \) mode, a mode pattern with in-phase lateral lobes, such as the TM\(_{31} \) pattern or the TE\(_{31} \) pattern, is needed. We can rule out the TE\(_{31} \) mode because its superposition with the TE\(_{12} \) mode forms a ring with four nodes and four antinodes. Hence Fig. 4(c) displays a superposition of the TM\(_{11} \) and TE\(_{12} \) modes.

The fact that the field pattern at \( \sim 7.5 \) ps for the AgI-coated waveguide is different from the uncoated waveguide is partly caused by a higher attenuation experienced by the TM\(_{11} \) mode due to the dielectric coating. This suggestion is supported by the effect of the dielectric layer on the attenuation coefficients [Fig. 2(b)]. The TM\(_{11} \) mode contains field lines terminating on the guide walls, and thus a portion of the mode energy is travelling within the dielectric in the AgI-coated waveguide. Therefore, the dielectric coating increases the attenuation of the TM\(_{11} \) mode, whereas the TE\(_{12} \) mode, with the field approaching zero near the metallic surface, makes it less sensitive to the dielectric coating. Hence the field pattern in the AgI-coated waveguide is more similar to the TE\(_{12} \) mode.

The detailed characterization of the mode structure presented here provides a further insight into waveguide mode imaging using CW THz sources or using the Fourier-transformed time-domain data. In the single frequency analysis, normal modes cannot be distinguished experimentally from multimode interference, similar to the example...
shown in Fig. 4(d). In the multimode operation, the output field (or intensity) pattern is therefore a superposition of all excited modes. Considering the normal modes determined in this study, we conclude that the TE_{11}⁻, TM_{11}⁻, and TE_{12}⁻ modes can be excited in the waveguide if the THz beam is centered on the waveguide axis. The output pattern therefore can take a form of any superposition of these modes.

As the first example, in Fig. 5(a) we show a combination of the fundamental modes at 3.2 THz for the AgI-coated waveguide (0.8930 × E_{x}^{TE_{11}} and −0.45 × E_{x}^{TM_{31}}) that is similar to the pattern of the low-loss HE_{11} mode [1,15,17–19,30,31]. If the HE_{11} mode pattern develops at the output aperture of the waveguide either from the fundamental HE_{11} mode or from the above combination, it is known to generate an intensity distribution with a Gaussian-like profile in the far field [6,14,20]. Notice that even at 3.2 THz, the frequency used in the CW experiment of [25], our numerical modeling shows the TE_{11}⁻ and TM_{11}⁻ like distributions because the dielectric coating is not thick enough to form the ideal low-loss HE_{11} mode.

To back up the above discussion, we perform a CW far-field mode imaging using a similar AgI-lined hollow metallic waveguide (140 mm long) [25]. Figure 6 shows that a Gaussian-like distribution is measured in the far field. It is important to note that this single CW experiment is not sufficient to determine if such a pattern has been originated from the HE_{11} mode or from a superposition of modes. Only after the near-field time-resolved analysis can we conclude that it is originated from the admixture TE_{11}⁻ + TM_{11}⁻. This example shows that the impact of the dielectric coating on the hollow metallic waveguides is difficult to determine using a single frequency experiment.

As the second example we consider a superposition of two mode profiles experimentally determined in the time-resolved measurements: −0.3 × E_{x}^{TE_{11}} and 0.9539 × E_{x}^{TE_{12}} [Fig. 5(b)]. The latter field pattern creates an intensity distribution similar to another important mode, the TE_{01} mode. As in the first example, CW experiment is not sufficient to determine if the pattern is caused by the TE_{01} mode or by a mode superposition. We note, however, that the latter ambiguity can be resolved using polarizers or polarization-sensitive detectors.

These examples demonstrate the importance of supplementing the mode images in multimode THz waveguides with the time-resolved waveguide mode imaging and numerical modeling. Applying similar analysis to the experimental results on AgI-coated waveguides in [25], in which the observed emission patterns suggested the presence of the HE_{11} mode, we conclude that the result may have been affected by mode interference.

In case the time-resolved characterization is not available, we can provide the following recommendations for waveguide mode characterization: (i) the length of the waveguide samples must be kept long enough so that only one or two modes maintain significant intensities; (ii) output patterns must be measured for several waveguide lengths to verify that the pattern remains independent of the length. In addition, a priori knowledge of the normal modes and the corresponding losses is essential.

We can also make the following recommendations for time-resolved characterization: (i) control of the input beam can help in transferring most of the energy into a single mode, as it was done in [31] and here; and (ii) frequency-narrower THz probing pulses can reduce the temporal overlapping modes because with the frequency-narrower pulses experience a smaller temporal broadening. This can be done either by a THz source with narrower frequency bandwidth or by placing an appropriate filter between the broadband THz source and the waveguide.
4. CONCLUSIONS

We characterized modes experimentally in Ag/AgI hollow metallic waveguides at THz frequencies, in the regime of ultrathin dielectric coating using the near-field imaging system combined with time-domain measurements. The experimental results are supplemented with electromagnetic simulations. For comparison purposes and for the sake of completeness, the identical methodology has been also applied to a well-known cylindrical hollow metallic waveguide. We show that in the THz frequency range (1–3.2 THz) the 1 μm thick layer of AgI on the waveguide inner walls is not sufficient to form the ideal low-loss HE₁₁ modes. The mode profiles for the lowest-order modes, as confirmed by numerical modeling, are more similar to the classical modes in the hollow metallic waveguide. We show here that, in order to bridge the gap between observations and understanding, it is extremely effective to combine THz near-field imaging, time-resolved measurements, and numerical electromagnetic modeling. With these complementary techniques, a complete picture of the problem can be captured, allowing one to identify unambiguously the modal structure in real THz waveguides in a multimode environment. The work is another step forward in the new but rapidly evolving subfield of THz near-field microscopy for waveguide characterization.

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